Abstract
The cost of manufacturing textile-reinforced composite aerostructures using Resin Infusion under Flexible Tooling (RIFT) can be reduced by computational modelling. This paper outlines the current progress and contributions made towards this goal.

A continuum-based material model was incorporated into a finite element package to simulate the draping of a dry carbon fibre fabric. It accurately tracks the changes in the warp and weft fibre orientations and has been experimentally validated. Material characterisation was performed to determine the tensile and shear properties of a plain weave fabric reinforcement material. In support of bias extension shear testing, an accessible Digital Image Correlation (DIC) approach was developed for accurate optical strain measurement. A relationship between permeability and shear angle was also experimentally determined using a novel permeability measurement technique.

Future work is planned to combine all these aspects in an infusion model and demonstrate the complete process model.

1 Introduction
The increasing use of composite materials in primary aircraft structures is driving demand for large and highly integrated parts in commercial aircraft. Resin Infusion under Flexible Tooling (RIFT) is an attractive process for these applications, as only one tool surface is required and it can be performed out-of-autoclave [1]. Textile reinforcement materials provide the ideal resilience and formability to be paired with liquid composite moulding techniques like RIFT, and are hence the focus of this research.

The RIFT process is not without its drawbacks however, with reliability and repeatability seen as problematic in the aerospace industry. This is because the process continues to rely on skilled and experienced operators, in what is essentially a trial and error approach. Therefore it is becoming desirable to simulate the process to overcome this problem and reduce the amount of wasted time and material on failed attempts.

The simulation of the RIFT process can be broken down into two major stages: draping, where dry reinforcement material is formed into the part shape; and infusion, where resin is drawn into the material and subsequently left to cure under pressure. Each stage has separately seen considerable study, though there have still been only limited attempts to create a complete process model for liquid composite moulding techniques such as RIFT [2].

The effectiveness of a draping model is generally judged by how realistically it simulates the reorientation of yarns during deformation. The angular reorientation of warp and weft yarns relative to their undeformed state is known as the shear angle, \( \gamma \), as illustrated in Fig. 1. This is the most appropriate parameter for monitoring shear deformation in textiles.

Kinematic simulation methods, such as the pin-jointed net and fishnet methods [3][4], were among the earliest approximations used, though these lack sophistication when it comes to complex geometries.
and often fail for bridged or concave part sections. On the other hand, highly detailed discrete and semi-discrete models have been developed with considerable success [5][6][7], often replicating the behaviour of individual fibres or yarns with simple elements. Continuum models are also showing a high degree of accuracy [8][9][10], despite the homogenisation of the complex fabric architecture compared with the discrete models.

A further consideration is that the permeability of the fabric material changes locally during draping, as yarns re-orient themselves under shear deformation. Studies have quantified this variation in permeability over the range of possible shear angles to be greater than 50% in some fabrics [14][15][16]. Thus it is important to couple the draping model results with the infusion simulation through the characterisation of material permeability over a range of shear angles.

This paper describes the progress and current contributions towards the creation of a complete process model under this project, highlighting developments in material characterisation and permeability testing.

2 RIFT Process Modelling

In order to create a complete process model for RIFT manufacturing, four key areas of research have been identified: the draping model, the supporting material characterisation, the shear angle and permeability relationship and the infusion model. The interaction of these components is visualised in Fig. 2.

![Flow chart for the full RIFT process model](image)

Material characterisation provides greater realism to the draping model, such that an accurate part geometry and shear distribution can be predicted for a complex layup. By establishing a relationship between shear deformation and permeability in a textile reinforcement material, the shear distribution that results from the draping model can be converted into a permeability distribution. This can then be combined with the deformed part geometry and fed into an infusion model.
into the infusion model to simulate the final stage of the RIFT process, and ultimately evaluate a potential infusion strategy.

At this stage, the first three major segments of this work have been performed, with only the development and implementation of the infusion model still to be completed under this project.

**3 Drape Modelling**

During RIFT manufacturing, draping is the preliminary stage for forming the fabric reinforcement into the desired shape. Hence it is particularly important to model this deformation accurately as all subsequent stages of the process rely on the results. In order to realistically simulate the material behaviour, the model needs to be able to accurately predict the reorientation of yarns during draping, and calculate shear angles. For these materials, deformation is dependent on the tensile and shear properties of the fabric.

A hypoelastic continuum method has been implemented, including a customised VUMAT material subroutine within Abaqus [17], based on those presented by other researchers [9][18]. This choice was made due to the accuracy and efficiency of continuum-based finite element approaches. The model has been developed for Abaqus/Explicit due to the degree of geometric and material non-linearity present in draping, where implicit solvers become inefficient.

Within the model, layers of fabric material are treated as continuous sheets of membrane elements (M3D4R), where the intricate effects of the underlying fabric architecture are incorporated as complex material behaviour in the VUMAT subroutine. An assumption is made on the independence of yarn tensile properties from the shear response of the fabric material, though both properties are able to be defined as non-linear functions. The material subroutine requires the definition of the constitutive model and tracks the non-orthogonal yarn orientations during deformation based on the orthogonal, planar strains and deformation gradient tensor available from Abaqus. The fundamental theory, on which the material subroutine is based, is described in detail by Peng et al. [19].

An ‘elbow’ shaped part has been modelled to demonstrate the draping model (shown in Fig. 3). Here it can be seen that the deformation in the model appears to agree well with a hand layup, and produces a complex shear distribution ranging from $-9^\circ$ to $40^\circ$ based on the material properties determined in the following section of this paper.

![Fig. 3. a) Experimental and, b) modelled draping of material over an ‘elbow’ shaped part (with contours representing the shear angle distribution).](image)

![Fig. 4. Comparison of material draw-in from experimental and modelling results for one corner of the ‘elbow’ shaped part.](image)
In Fig. 4 the simulated profile for one corner of the fabric edge is compared to results from experimental draping. The VUMAT subroutine model can be seen to accurately predict the draw-in of the material. A similar model was run without tracking fibre directions, simplified to a purely orthogonal basis. As it can be seen in Fig. 4, this orthogonal model is not as successful: underestimating the material draw-in in the edge regions most affected by shearing (as seen in Fig. 3).

Further quantitative analysis of the draping model has been performed by replicating work from published literature [9][10]. For both ‘hemispherical’ and ‘double dome’ cases, the presented model showed very good agreement with the experimental and simulation results provided.

4 Material Characterisation

In support of the draping model, characterisation of the fabric reinforcement provides a measure of the realistic material behaviour for simulation. As the tensile and shear properties of woven fabrics are the most important to the draping process, the VUMAT subroutine requires definition of warp and weft tensile moduli, $E_1$ and $E_2$, and the in-plane shear modulus, $G_{12}$.

To this end, appropriate test methods have been developed for both tensile and shear testing of fabric reinforcement materials. Specifically for this project, an aerospace grade, carbon fibre, plain weave fabric with 3K tows and a 0.193 kg/m$^2$ areal density has been used. However, the testing and modelling process employed is applicable for any woven fabric reinforcement material with a repeatable geometry.

There are a number of challenges in testing textile materials, primarily the loose nature of the material that facilitates unravelling, fraying and yarn slippage during handling. Cutting and mounting of material samples must be performed with great care in order to preserve the state of the fabric architecture and yarn orientations prior to testing. Due to these complications, and the complexity of the material itself, there is a general lack of standardisation in the field, and a variety of competing experimental techniques are commonly used to determine both properties.

4.1 Tensile testing

4.1.1 Tensile test method

Due to the nature of the fabric reinforcement material, standard tensile coupon tests are not applicable and alternative methods need to be employed. As previously noted, these materials are prone to damage and deformation during handling. However, there are also further challenges specific to tensile testing. For carbon fibre fabrics in particular, tensile loads are high, meaning that correspondingly high clamping forces are required to prevent test specimen slippage. There are a few competing approaches, though relatively complex biaxial testing is popular for tensile property characterisation due to the interaction between the warp and weft yarns of a fabric [20]. Even though uniaxial tensile test methods do not account for this crimp interchange, in the absence of any standardised biaxial tests, the ASTM tensile ‘strip’ standard [21] has been employed.

Under the standard specifications, tensile samples were cut to have a $75 \times 75$ mm gauge area with a $25 \times 50$ mm clamping section above and below. Subsequently yarns were removed from the free edges of the gauge area such that only the vertical yarns within the clamping width of the specimen remained. This ‘ravelling’ process ensured that the yarns being loaded were less influenced by edge effects and that transverse yarns did not slip out from the longitudinal yarns under loading. The width of the gauge section meant that testing was performed across 13 yarns in each sample.

Samples were cut in both the 0° and 90° orientations to ensure that both warp and weft fibre directions were tested. Testing of the samples was conducted on an Instron 4505 frame with updated 5500R electronics, using a 5 kN load cell under a 0.5 mm/min constant rate of extension.

4.1.2 Strip test results

The tensile strip tests were successful as the clamps used to hold specimens (shown in Fig. 5) prevented any slippage from occurring. From Fig. 6 it can be seen that the tensile modulus of fabric samples is initially non-linear up to 0.002 strain, after which it tends towards a linear 15 GPa for both 0° and 90° specimens. This early non-linearity can be explained by the de-crimping of longitudinal yarns, i.e., straightening from their initially undulating configuration under loading. Once straight, the full
tensile strength of these longitudinal yarns provides the steep and near linear behaviour expected from carbon fibres. As seen in Fig. 5, the straightening of these longitudinal yarns consequently increases the waviness of the transverse yarns, such that they splay out alternatively at the free edges.

![Fig. 5. a) Tensile strip test and, b) close up view.](image)

which yarns become ‘locked’ and resistance to shear deformation greatly increases. Since shearing loads are so small in the undeformed state, mechanical tests are particularly sensitive to manual handing, which poses further difficulty in the selection of an appropriate method.

One shear testing approach is the Kawabata simple shear test [22], though it is typically limited to a lower range of shear deformation [23]. Alternatively, the ‘picture frame’ test has seen greater success, where square or cruciform shaped samples are clamped into a deformable diamond shaped rig [24]. This test method often requires a complex set-up for which fabric samples can be difficult to clamp and align [25]. A third method, the ‘bias extension’ test, shows similar capability to the ‘picture frame’ approach and operates in the same fashion as uniaxial tensile tests. However, rectangular samples are cut and oriented in the ‘bias’ direction, such that the warp and weft yarns are ±45° relative to the loading direction.

Despite work by an international collaborative effort to establish benchmarks [26], there remains no standardised method for the shear testing of fabric materials. With the majority of literature recommending either the picture frame or the bias extension test, the latter was selected due to the simplicity of the requisite rig.

Similar to the tensile testing, shear testing was performed with a Constant Rate of Extension (CRE) control. However, as a higher resolution and accuracy was desired for lower loads, testing was performed on an Instron 5948 MicroTester machine with a 100 N load cell. A loading rate of 10 mm/min was used for these tests, as is common, since results are generally rate independent [27]. The gauge area of specimens was 50 × 100 mm, facilitating a central diamond region comprising 18 × 18 yarns as shown in Fig. 7.

![Fig. 6. Tensile stress-strain curves from experimental strip testing.](image)

4.2.2 Optical strain measurement

Though the method appears to be relatively basic, it can be particularly difficult to measure shear deformation in the bias extension test, as the sample is not entirely sheared uniformly. Historically this was a major issue and theoretical calculations, purely based on the ideal experimental kinematics, had to be used. With the current availability of
digital imaging though, mechanical test methods are increasingly incorporating optical strain measurement techniques. Digital Image Correlation (DIC) is one such technique that has been employed to overcome the shortcomings of the bias extension test method, and provides greater accuracy to the experimental measurement of shear.

Typically specialised software and cameras are used for calculating strain with DIC, however a Matlab code has been developed in-house that correlates concurrent images from a sequential series taken during mechanical testing. A grid of ‘correlation points’ are tracked from image to image, enabling the measurement of nodal displacements. This changing grid is used to form isoparametric, bi-quadratic, nine-node elements for which the deformation gradients are calculated. Using a method of polar decomposition and a non-orthogonal basis that tracks yarn directions (similar to the material subroutine in the draping model) the shear angle is determined. This code is available on the MathsWorks File Exchange website and was based on a package for axial strain DIC developed by Cristoph Eberl [29].

4.2.3 Bias extension results and determination of the shear modulus

In order to evaluate the validity of the DIC results, values were compared with manually measured shear angles from the images taken during bias extension testing. As can be seen in Fig. 8, the DIC results showed very good agreement with measured values of shear angle. It should be noted that once shear locking was observed above 50°, the manual measurement of shear angles became susceptible to an error of ±2° as yarn orientations became difficult to distinguish with the human eye.

Raw loading and extension data from mechanical testing was coupled with the shear angle data from DIC in order to determine an appropriate curve for the shear modulus as a function of shear angle. This data was employed for theoretical calculations in an idealised case; assuming shear angle to be uniform in each region, with no shear in the triangular regions adjacent to the clamps. The shear angle in the central diamond region was also assumed to be twice that of the triangular zones that are between the central and clamped zones.

A shear force, normalised by central shear zone edge length, can be calculated and expressed in terms of shear angle, \( \gamma \), loading force, \( F \), specimen gauge height, \( H \), and gauge width, \( W \), according to theory outlined by Cao et al. [26].

\[
F_{sh}(\gamma) = \frac{1}{(2H - 3W) \cos \gamma} \left( \left( \frac{H}{W} - 1 \right) F \left( \cos \frac{\gamma}{2} - \sin \frac{\gamma}{2} \right) - WF_{sh} \left( \frac{\gamma}{2} \cos \frac{\gamma}{2} \right) \right) \tag{1}
\]

Though, since Eq. 1 is a function of the half shear angle, it becomes an iterative process to calculate the full range of force-shear curves based on the initial assumption in Eq. 2.

\[
F_{sh} \left( \frac{\gamma}{2} \right) = \frac{F_{sh}(\gamma)}{2} \tag{2}
\]

Subsequent values of shear force at half shear angle are simply interpolated between known values.

Then to calculate the shear stress, the normalised shear force needs to be multiplied by the edge length of the central shear zone, and divided by its area as shown in Eq. 3.

\[
\tau(\gamma) = \frac{WF_{sh}(\gamma)}{A} = \frac{2F_{sh}(\gamma)}{\sqrt{2}W} \tag{3}
\]

Lastly, an exponential function was fitted to this curve and differentiated to find the theoretical tangent shear modulus function based on experimental force and shear angle data (Eq. 4).

\[
G_{12}(\gamma) = 0.008196e^{4.24\gamma} + 2.5017 \times 10^{-10}e^{23.69\gamma} \tag{4}
\]

In order to validate this shear modulus for modelling purposes, a simulation of the bias extension test was conducted using the draping model with these experimentally determined material properties.

Although the model is not able to replicate yarn slippage, the results show very good agreement with the experimental results shown in Fig. 8. Also, qualitatively the comparison shown in Fig. 7 reveals good agreement between the experimental DIC results and the modelling results at 15 mm extension, where both are shown on the same contour scale.
5 Permeability and shear angle relationship

5.1 Experimental approach

With a draping simulation that can accurately track yarn orientations and predict the shear angle distribution across an entire part, these results need to be translated to a distribution of permeability for subsequent infusion modelling. This is done by relating shear deformation in the fabric material with permeability change. In order to quantify this link over a range of shear angles, two approaches are possible: experimental permeability characterisation or predictive permeability modelling.

Despite extensive study in the area over the years, there are no standardised methods to experimentally determine permeability for textile reinforcements.

Recent efforts to benchmark common approaches ultimately found that tests carried out under similar conditions exhibited significantly scattered results [13]. Predictive methods, on the other hand, are relatively new and still rely on supportive experimental tests for validation. Hence, an experimental approach has been undertaken for this research.

Even though linear flow experiments are generally considered to exhibit less variability[30], an unsaturated radial flow experiment is preferred since the principal permeability directions are not known prior to testing at the various shear angles. This approach also allows for the collection of more data from a single test, facilitating permeability calculations in every direction to better describe the anisotropic flow.

Experiments were run under a constant injection pressure, rather than a constant inlet velocity, because the latter approach often requires unreasonably high pressure gradients. For this study the pressure differential across the system was imposed by drawing a vacuum at the outlet, with an oil reservoir open to ambient conditions. The permeability test set-up is shown in Fig. 9, where it can be seen that the test sample was sandwiched between a glass plate and a polycarbonate caul plate, with white breather cloth placed around the periphery to ensure an even vacuum within the test cavity.

Single plies of the plain weave carbon fibre fabric were tested in batches of at least six samples at various shear angles from 0° to 40° (where the natural shear locking state of the fabric occurs at around 45°-50°). Through-thickness flow and gravitational effects were neglected since the perform was only one ply thick, and testing was considered solely in 2D. Samples were 300 × 300 mm in their undeformed configuration, and the circular inlet port was 6 mm in diameter to minimise the effects of a circular inlet on an elliptical flow front [31]. The fluid used for these tests was a Newtonian oil, assumed to be incompressible, isothermal and chemically inert for the duration of the permeability tests.
5.2 Permeability calculation

The primary measurements from testing were taken with a digital video camera from below the glass plate with the radial flow pattern recorded as a function of time. This method was used in preference over alternative sensor methods that are often more difficult to set up, yield limited data, and may even negatively influence fluid flow through the test cavity [31]. As discussed in the literature [13], alternative measurement techniques can use fibre optic sensors, thermistors, pressure transducers, ultrasound, or electrical resistance measurements. However using digital video does not require prior knowledge of the principal permeability directions, and also provides greater flexibility in post processing and analysis, since the full field of flow front data, as a function of time, is readily available.

Video from the experiments were processed to track the advancing flow front in all directions. Based on the theory discussed by Weitzenböck et al. [31][32] this allowed the calculation of permeability for every direction, \( K_i' \), rather than a finite few (Eq. 5).

\[
K_i' = \frac{\mu \varepsilon}{4\Delta P} F_i
\]  

(5)

Where \( \mu \) is the fluid viscosity, \( \varepsilon \) is the material porosity, \( \Delta P \) is the pressure gradient and \( F_i \) is the linear regression of the term \( N_i \) against time, defined in Eq. 6.

\[
N_i = \left( R_{f,i}^2 \left( 2 \ln \left( \frac{R_{f,i}}{R_{o,i}} \right) - 1 \right) + R_{o,i}^2 \right)
\]  

(6)

Here \( R_{f,i} \) is the flow front radius in the ‘i’ direction and \( R_{o,i} \) is the inlet radius.

The video processing and subsequent calculations were automatically performed within a novel Matlab script that has been developed in-house to produce a radial permeability distribution.

5.3 Permeability and shear angle results

The relationship between shear angle, flow direction and permeability shown in Fig. 10 reveals a near isotropic state at 0° shear angle as is expected for a balanced plain weave fabric. Anisotropy then increases with shear angle, until there is a factor of five difference between principal permeability values at 40° shear.

For each shear angle tested, local maxima and minima represent the principal permeability values, \( K_1 \) and \( K_2 \) respectively. From Fig. 10, the principal permeability directions are clearly seen to be consistent for every shear angle. Permeability values at 10° shear are seen to increase for all flow directions which appears to contradict the trend of \( K_1 \) values increasing and \( K_2 \) values decreasing from the 0° shear isotropic state with increasing shear angle.

Fig. 10. Surface plot of the relationship between shear angle and permeability for various flow directions.
6 Discussion

The tensile strip test method undertaken in this work assumes that the warp and weft yarn properties are independent. However, it is known that this is not the case in reality. Biaxial testing is one way to compensate for the interaction between the yarns, though it requires more exhaustive testing of the material under a range of different loading ratios, or some form of predictive modelling [33]. Though this is quite significant for processes such as thermoforming, the effect of this interaction is expected to be minimal in RIFT manufacturing.

The use of the bias extension test for shear characterisation has been employed primarily for its relative simplicity. However, the picture frame test could easily be used instead, with only minor changes necessary for the DIC code that has been developed in-house. This would help overcome any concerns with slippage that occurs in the later stages of bias extension testing, but might introduce issues with pre-tensioning, clamping and alignment. More recently, there has even been biaxial bias extension testing performed to look at the coupling of shear and tensile properties [34], which may be worth pursuing.

In the experimental characterisation of permeability, work concentrated on single ply tests as they are expected to show better repeatability than those with multiple plies. Thicker samples introduce nesting, gravitational and 3D flow effects which are likely to produce a greater scatter in results between similar tests. Results presented in this work were found to be quite repeatable, however the trend of increasing permeability with increasing shear angles appears to be contrary to much of the literature [15][16]. This is due to the relatively high porosity in a single ply of the plain weave material. It is hypothesised that the alignment of yarns at higher shear angles facilitates not only capillary flow but also aligns ‘channels’ for flow in these directions, which may actually be closed off in materials with a lower porosity. However, the aim of much of the presented work at this stage has been more a demonstration of process capability.

As the ultimate goal of this project is to create a process model capable of minimising experimental testing during part development, it may also be worth pursuing predictive modelling methods for characterising tensile, shear and permeability properties in the future.

7 Conclusion

With the aim of producing a complete predictive model for Resin Infusion under Flexible Tooling (RIFT), work has been contributed to several key areas.

A successful continuum-based draping model was implemented, including a hypoelastic and non-orthogonal material subroutine that accurately tracks fibre directions during deformation. In support of this model, the tensile modulus of a plain weave carbon fibre fabric has been characterised through uniaxial ‘strip’ testing. Bias extension shear characterisation has also been performed using a Digital Image Correlation approach for optical strain measurement that has been developed in-house. Similarly, a novel approach for flow front tracking and the calculation of permeability has also been developed in Matlab for experimental permeability testing. This approach has been used to determine the relationship between shear angle, permeability and flow direction in the same carbon fibre plain weave material.

Work is planned to ultimately combine all these aspects into an infusion model for the RIFT process.

References


[31] J R Weitzenböck, R A Shenoi, and P A Wilson, "Radial flow permeability measurement. Part A:

